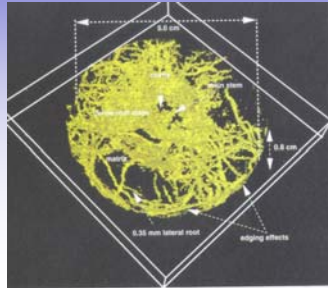


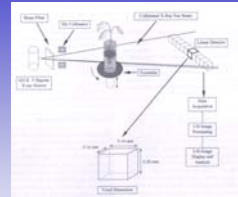
**Estimation of Multi-Dimensional Root Water and Nutrient Uptake Rates under Time-Varying Soil Moisture Conditions**

(2002, *Advances Agronomy*, Vol 77)

Jan W. Hopmans and colleagues  
University of California, Davis



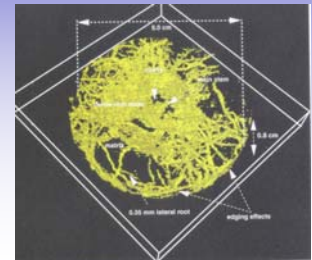
**Example of CMT for nondestructive 3D plant root measurements**



**Experimental Setup**

Heeraman, Hopmans and Clausnitzer  
*Plant & Soil*, 1997

**3D Root Image**



**ROOT FUNCTIONING OF WATER & NUTRIENT UPTAKE:**

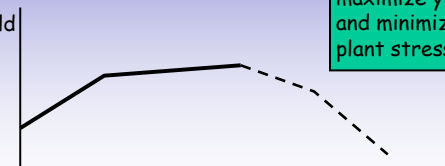
**HISTORICAL POINT-OF-VIEW**

**OUT-OF-SIGHT = OUT-OF-MIND**  
(Clothier and Green, 1997)

**RESULT:**

**MOSTLY EMPIRICAL RELATIONSHIPS BETWEEN CROP YIELD AND RESOURCE AVAILABILITY**

Grain yield (ton ha<sup>-1</sup>)



**GOAL:**  
maximize yield and minimize plant stress

N or water application

## KNOWLEDGE GAP ON PLANT RESPONSE OF WATER AND NUTRIENT LIMITATIONS TO CROP PRODUCTION

### THIS IS IMPORTANT

INCREASINGLY, CONSTRAINTS BECAUSE OF :

- WATER LIMITATIONS
- ENVIRONMENTAL CONCERNS

#### EXAMPLES:

- Micro-irrigation and Fertigation
- Deficit Irrigation and Partial root zone drying
- Agroforestry
- Bioremediation and Phytoremediation

#### CURRENT NEED:

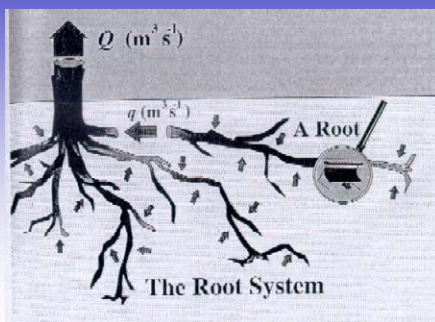
COMBINE SOIL WITH PLANT EXPERTISE,  
TO BETTER UNDERSTAND CONCEPTS AND  
PROCESSES OF WATER AND NUTRIENT  
STRESSES ON CROP GROWTH

SINCE THE REALITY IS THAT BOTH SOILS AND  
ROOTS ARE HETEROGENEOUS

AND

BOTH WATER AND NUTRIENT DISTRIBUTION ARE  
VARIABLE IN BOTH SPACE AND TIME

Overall root transport is controlled by  
local variations in root water and nutrient  
uptake

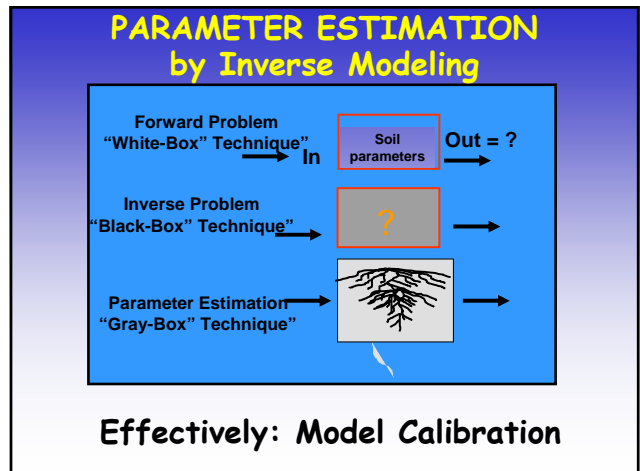
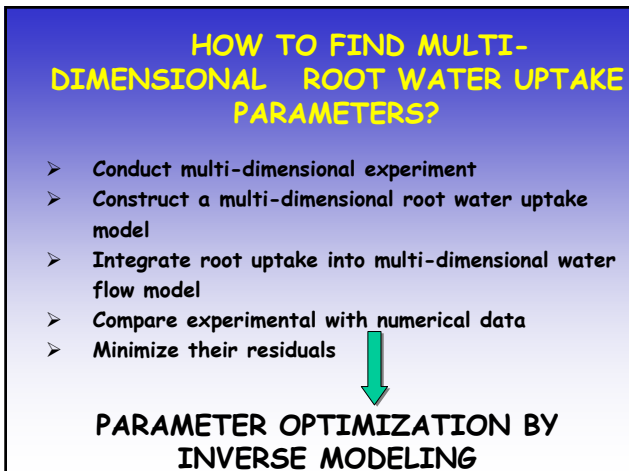
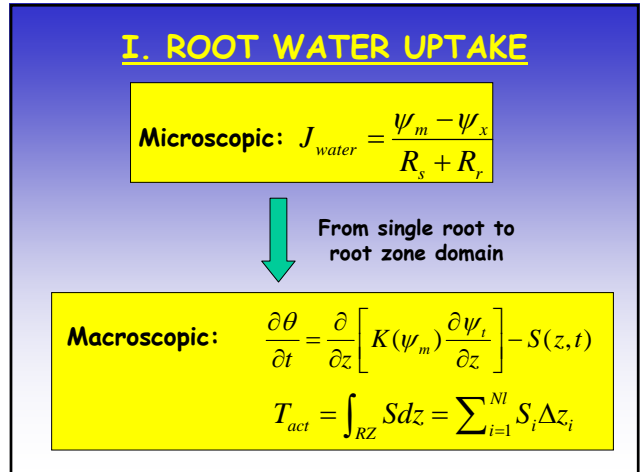
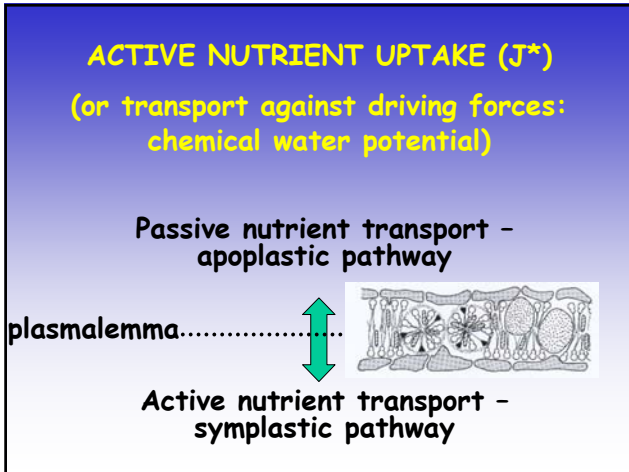


Clothier and Green, 1997

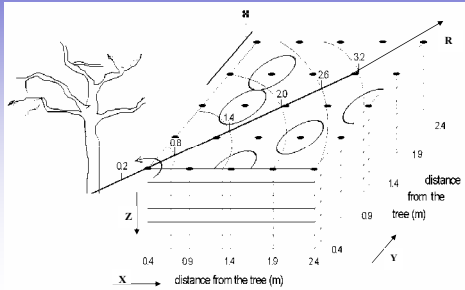
#### Progress requires:

- Multi-dimensional modeling approach.
- Understanding of plant's response to spatially-distributed soil water and plant-available nutrients, ???
- Additional experimental data





## EXPERIMENTAL LAYOUT OF THREE-DIMENSIONAL SOIL MOISTURE MEASUREMENTS (ALMOND TREE)



## Multi-dimensional root water uptake & soil hydraulic parameters

(Vrugt, Hopmans and Simunek, SSSAJ and Water Resources Research)

Solve unsaturated water flow equation for three-dimensional soil domain, with root water uptake term (S)

$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial x_j} \left[ K (K_{ij}^A \frac{\partial \psi_m}{\partial x_j} + K_{ij}^A) \right] - S(x, y, z)$$

SIMULATION MODEL:  
HYDRUS-3D

## MULTI-DIMENSIONAL ROOT WATER UPTAKE MODEL

$$RDF(x, y, z) = \left(1 - \frac{x}{X_m}\right) \left(1 - \frac{y}{Y_m}\right) \left(1 - \frac{z}{Z_m}\right) e^{-\left(\frac{P_x}{X_m}|x^2+y| + \frac{P_y}{Y_m}|y^2-x| + \frac{P_z}{Z_m}|z^2-x|\right)}$$



$$S_{max}(x, y, z) = \frac{X_m Y_m RDF(x, y, z) T_{pot}}{\int_0^{X_m} \int_0^{Y_m} \int_0^{Z_m} RDF(x, y, z) dx dy dz}$$

Unstressed Normalized Root Water Uptake, at a point

## Water Uptake under Water-Stressed Conditions

Water Stress Response Function

$$\alpha(\psi_m) = \frac{1}{1 + \left(\frac{\psi_m(x, y, z, t)}{\psi_{m,50}}\right)^p}$$

Actual Water Uptake:

$$S(\psi_m, x, y, z) = \alpha(\psi_m) S_{max}(x, y, z)$$

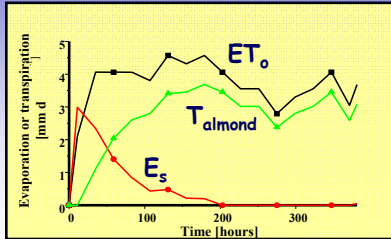
Actual Plant Transpiration:

$$T_{actual} = \frac{1}{X_m Y_m} \int_0^{X_m} \int_0^{Y_m} \int_0^{Z_m} S(\psi_m, x, y, z) dx dy dz$$

## Computation of $T_{pot}$

$$T_{pot,almond} = ET_{almond} - E_s$$

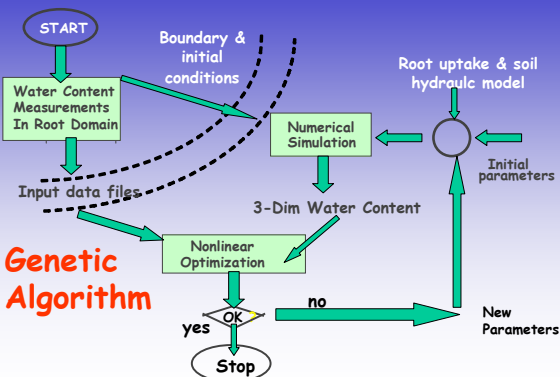
$$ET_{almond} = K_c ET_0$$



## PARAMETER OPTIMIZATION OF THREE-DIMENSIONAL ROOT WATER UPTAKE MODEL

- Obtain field measurements of multi-dimensional soil moisture during a 2-week monitoring period;
- Simulate multi-dimensional soil moisture distribution, using transient HYDRUS-3D model;
- Optimize root water uptake & soil hydraulic parameters using inverse modeling, minimizing residuals of measured and simulated water contents

## Inverse Modeling of Root Water Uptake



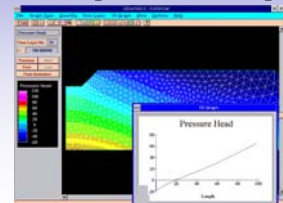
## MODELING

### Van Genuchten-Mualem & HYDRUS

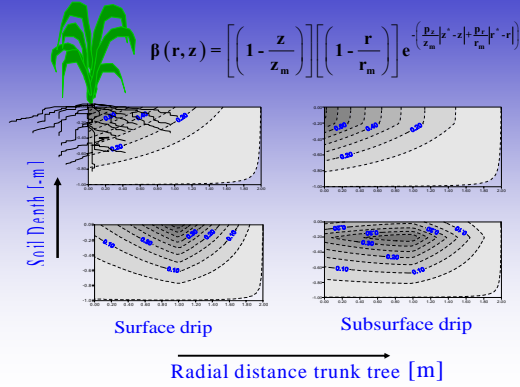
$$S_e = \left[ \frac{1}{1 + (\alpha h)^n} \right]^m$$

$$K_r = S_e^l \left[ 1 - \left( 1 - S_e^{1/m} \right)^m \right]^2$$

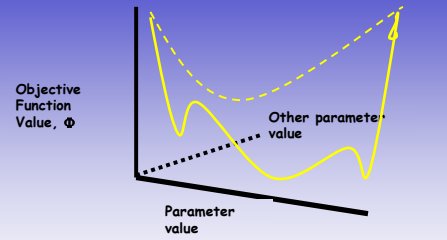
SIMULATION MODEL:  
HYDRUS-3D



### Flexibility of two-dimensional root water uptake model



### Optimization - Minimize Objective Function

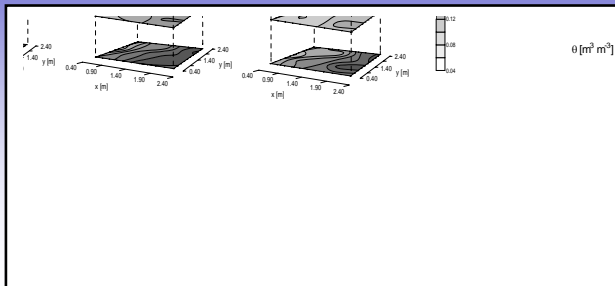


$$\Phi(\mathbf{p}, \theta) = w_i \sum_{i=1}^n \left[ \theta^s(\mathbf{x}, t_i) - \theta(\mathbf{x}, t_i, \mathbf{p}) \right]^2$$

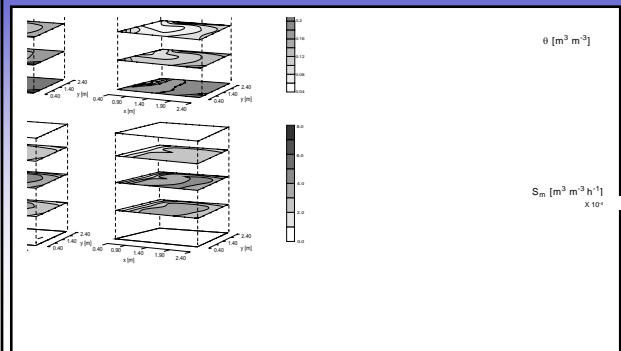
$\mathbf{p}$ : vector with optimized parameters

### THREE-DIMENSIONAL SOIL MOISTURE OBSERVATIONS

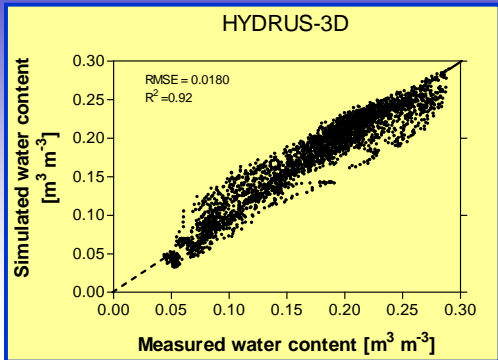
(Vrugt et al., 2001)



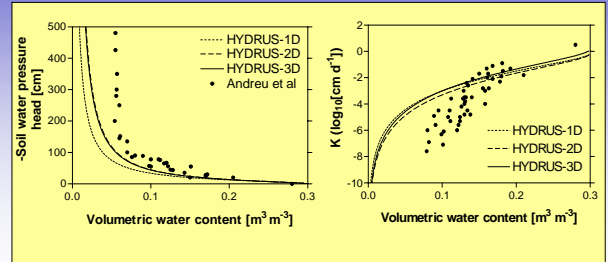
### SIMULATED THREE-DIMENSIONAL SOIL MOISTURE AND ROOT WATER UPTAKE DISTRIBUTION



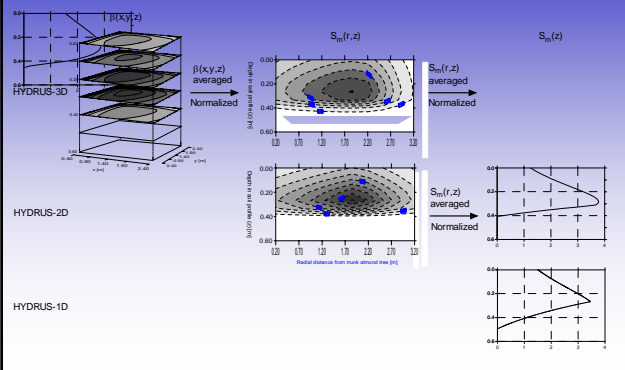
### Simulated (after optimization) versus Measured Water Content



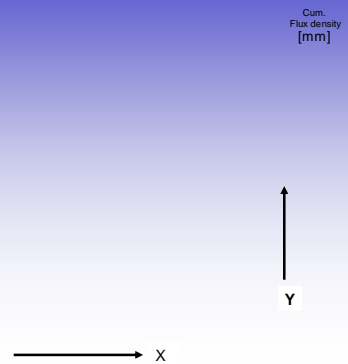
### Soil hydraulic functions, for instrumented field plot



### Comparison of one-, two- and three-dimensional uptake distributions



### Multi-dimensional root water uptake may have enormous influence on spatial and temporal variability of root zone leaching





## II. ROOT NUTRIENT UPTAKE

**Microscopic:**  $J^* = \frac{J_{\max}^* \cdot (c - c_{\min})}{K_m + (c - c_{\min})}$

From single root to root zone domain

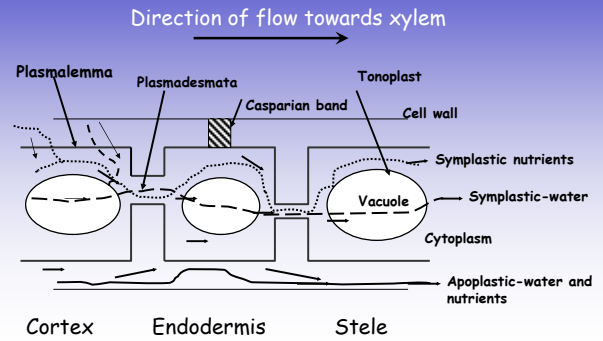


Active nutrient uptake:  
 $N_i = RDFN_i J_i^*$

**Macroscopic:**  $\theta \frac{\partial c}{\partial t} = \frac{\partial}{\partial x_i} \left( \theta D_{ij} \frac{\partial c}{\partial x_j} \right) - J_{w,i} \frac{\partial c}{\partial x_i} - S'$

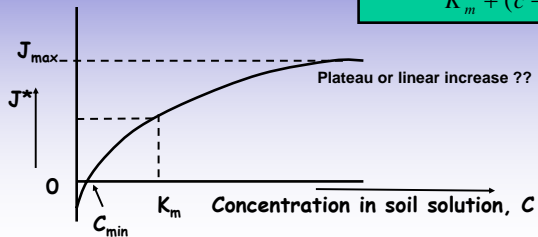
For each compartment  $i$ , partition between passive and active uptake:  
 $S'_i = f_1 S_i c_i + f_2 N_i$

## PATHWAYS FOR WATER AND NUTRIENT THROUGH PLANT ROOT

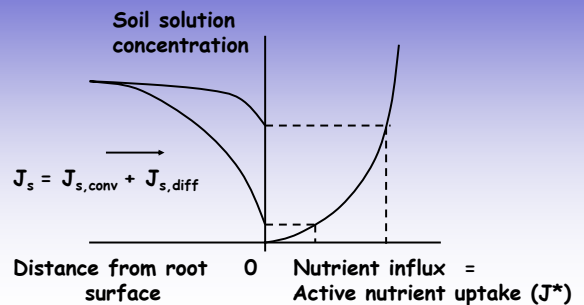


ACTIVE TRANSPORT IS CONSIDERED EQUIVALENT TO ENZYME KINETICS (MICHAELIS-MENTEN)

$$J^* = \frac{J_{\max}^* \cdot (c - c_{\min})}{K_m + (c - c_{\min})}$$



## SUPPLY-CONTROLLED ACTIVE NUTRIENT UPTAKE



## PARTITION NUTRIENT UPTAKE BETWEEN PASSIVE AND ACTIVE UPTAKE

$$S' = f_1 S_c + f_2 N$$

$S'$  - Total nutrient uptake

$S_c$  - Passive nutrient uptake (with water uptake - apoplastic pathway)

$N$  - active nutrient uptake (symplastic pathway)

$f_1$  and  $f_2$  - may be a function of nutrient availability and plant nutrient demand or deficit

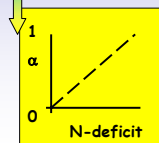
Define active nutrient uptake ( $N$ ) using RDFN (as water uptake), to characterize distribution of active uptake sites

$$(S' = f_1 S_c + f_2 N)$$

$$N_{pot} = \int_{RZ} J^* \quad N_{max,i} = RDFN_i \times N_{pot}$$

$$N_i = \alpha(\text{plant N deficit}) \times N_{max,i}$$

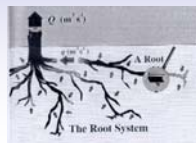
$$N_{act} = \int_{RZ} N_i$$



## RECOMMENDATION 1

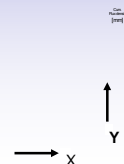
The overall functioning of the plant is controlled by local variations in uptake rates.

Research is needed to integrate local uptake variations to total plant uptake as a function of soil environmental factors (water and nutrient stresses),



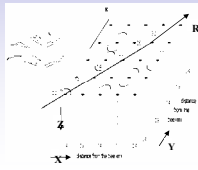
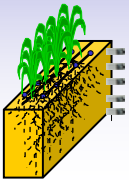
## RECOMMENDATION 2

A multi-dimensional approach is essential to improve model predictions of plant response to water and nutrient stresses and nutrient loads to the groundwater

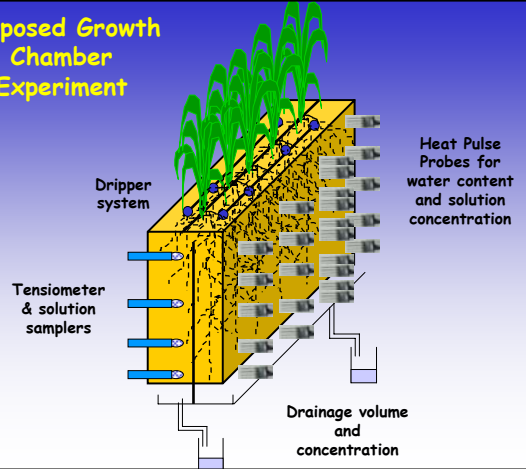


### RECOMMENDATION 3

Dedicated experiments are needed to test and calibrate multi-dimensional root water and nutrient uptake models, and to better understand the partitioning between passive and active nutrient uptake



### Proposed Growth Chamber Experiment



### NEW Heat Pulse Probe DESIGN

- To measure:
- Soil thermal properties
  - Soil water content
  - Bulk soil and solution EC
  - Darcy water flux
  - Solute dispersivity

